

Mark Scheme (Results)

January 2012

International GCSE Mathematics
(4MA0) Paper 4H

Edexcel and BTEC Qualifications

Edexcel and BTEC qualifications come from Pearson, the world's leading learning company. We provide a wide range of qualifications including academic, vocational, occupational and specific programmes for employers. For further information, please call our GCE line on 0844 576 0025, our GCSE team on 0844 576 0027, or visit our qualifications website at www.edexcel.com. For information about our BTEC qualifications, please call 0844 576 0026, or visit our website at www.btec.co.uk.

If you have any subject specific questions about this specification that require the help of a subject specialist, you may find our Ask The Expert email service helpful.

Ask The Expert can be accessed online at the following link:

<http://www.edexcel.com/Aboutus/contact-us/>

Pearson: helping people progress, everywhere

Our aim is to help everyone progress in their lives through education. We believe in every kind of learning, for all kinds of people, wherever they are in the world. We've been involved in education for over 150 years, and by working across 70 countries, in 100 languages, we have built an international reputation for raising achievement through innovation in education. Find out more about how we can help you and your students at:

www.pearson.com/uk

January 2012

Publications Code UG030750

All the material in this publication is copyright

© Pearson Education Ltd 2012

January 2012 International GCSE Mathematics (4MA0) Paper 4H Mark Scheme

Apart from Questions 3, 13(b) and 17(f) (where the mark scheme states otherwise), the correct answer, unless clearly obtained by an incorrect method, should be taken to imply a correct method.				
Question	Working	Answer	Mark	Notes
1.	$\frac{4.2}{1.12}$		2	M1 for 4.2 or 1.12 or 0.6 or $\frac{15}{4}$
		3.75		A1
				Total 2 marks
2.	$\frac{135}{180}$		3	M1
	0.75 oe			A1
		45		A1 cao
				Total 3 marks

3.	$4x = 7$ or $4x = 2 + 5$ or $7x - 3x = 7$ oe or $4x - 7 = 0$ oe		3	M2 for correct rearrangement with x terms on one side and numbers on the other AND collection of terms on at least one side or for $4x - 7 = 0$ oe M1 for $7x - 3x = 2 + 5$ oe ie correct rearrangement with x terms on one side and numbers on the other
		$1\frac{3}{4}$ oe		A1 Award full marks for a correct answer if at least 1 method mark scored
				Total 3 marks

4.	1 7 7		3	B2 for 1 7 7 in any order B1 for three positive whole numbers with either a median of 7 or a sum of 15 SC Award B1 for 0 7 8
		6		B1 cao
				Total 3 marks

5.	One correct point plotted or stated		4	B1 May appear in table
	2nd correct point plotted or stated			B1 May appear in table
	Correct line between $x = -2$ and $x = 4$			B2 B1 for a line joining two correct, plotted points
				Total 4 marks

6.	(a)	$1 + 7$ or 8		2	M1 8 may be denominator of fraction or coefficient in an equation such as $8x = 32$	SC If M0 A0, award B1 for 4 : 28
			28		A1 cao	
	(b)	32×45 or 1440 or 14.4(0)m		3	M1	
		$\frac{"1440"}{72}$			M1 dep	
			20		A1 cao	
					Total 5 marks	

7.	Fully correct factor tree or repeated division or 2, 2, 2, 5, 5 or $2 \times 2 \times 2 \times 5 \times 5$		3	M2 M1 for factor tree or repeated division with 2 and 5 as factors
		$2^3 \times 5^2$		A1 Also accept $2^3.5^2$
				Total 3 marks

8.	$y^{3+n-1} = y^6$ oe or $y^{3+n} = y^7$ oe or $3 + n - 1 = 6$ oe or $y^n = \frac{y^7}{y^3}$ or $y^n = \frac{y^6}{y^2}$ or $y^n = y^4$		2	M1	SC if M0, award B1 for an answer of y^4
		4		A1 cao	
				Total 2 marks	

9.	(a)	Complete, correct expression which, if correctly evaluated, gives 48 eg $4 \times \frac{1}{2} \times 6 \times 4$, $2 \times \frac{1}{2} \times 12 \times 4$, $\frac{1}{2} \times 12 \times 8$		3	M2 M1 for correct expression for area of one relevant triangle eg $\frac{1}{2} \times 6 \times 4$, $\frac{1}{2} \times 6 \times 4 \sin 90^\circ$, $\frac{1}{2} \times 8 \times 6$, $\frac{1}{2} \times 12 \times 4$
			48		A1 cao
	(b)	$4^2 + 6^2 = 16 + 36 = 52$		3	M1 for squaring and adding
		$\sqrt{4^2 + 6^2}$			M1 (dep) for square root
			7.21		A1 for answer which rounds to 7.21 (7.211102...)
					Total 6 marks

10.	(i)		$-1\frac{1}{2} < x \leq 2$	4	B2 Also accept $-\frac{3}{2} < x \leq 2$ or answer expressed as two separate inequalities B1 for $-1\frac{1}{2} < x$ or $-\frac{3}{2} < x$ or $x \leq 2$ (these may be as part of a double-ended inequality) or $-\frac{6}{4} < x \leq \frac{8}{4}$
	(ii)		-1 0 1 2		B2 B1 for 4 correct and 1 wrong or for 3 correct and 0 wrong
					Total 4 marks

11.	(a)	$75 = 3 \times 5^2$ and $90 = 2 \times 3^2 \times 5$ or 1,3,5,15,25,75 and 1,2,3,5,6,9,10,15,18,30,45,90 or 3×5		2	M1 Need not be products of powers; accept products or lists ie 3,5,5 and 2,3,3,5 Prime factors may be shown as factor trees or repeated division
			15		A1
	(b)	$2 \times 3^2 \times 5^2$ oe eg $6 \times 3 \times 5^2$ or 75,150,225,300,375,450 and 90,180,270,360,450		2	M1 Also award for $\frac{75 \times 90}{15}$
			450		A1
					Total 4 marks

12.	(a)		Rotation	3	B1	These marks are independent but award no marks if the answer is not a single transformation
			90°		B1 Also accept quarter turn or -270° (B0 for 90° clockwise)	
			(0, 0)		B1 Also accept origin, <i>O</i>	
	(b)		R correct	1	B1	As for (a)
	(c)		Rotation 90°	2	B1 Accept quarter turn or -270° instead of 90°	
			(3, 1)		B1 fit from their R if it is a translation of the correct R	
						Total 6 marks

13. (a)	$4y = 10 - 3x$ or $-4y = 3x - 10$		3	M1 May be implied by second M1 or by $y = -\frac{3}{4}x + c$ even if value of c is incorrect. or finds coordinates of 2 points on the line eg $(0, 2.5)$, $x = 2, y = 1$, table, diagram.
	$y = \frac{5}{2} - \frac{3}{4}x$ oe or $y = \frac{10}{4} - \frac{3}{4}x$ oe or $y = \frac{10 - 3x}{4}$ oe			M1 or for clear attempt to evaluate $\frac{\text{vert diff}}{\text{horiz diff}}$ for their pts
		$-\frac{3}{4}$		A1 Award 3 marks for correct answer if either first M1 scored or no working shown. SC If M0, award B1 for $-\frac{3}{4}x$

13	(b)	eg $9x + 12y = 30$ $10x - 12y = 46$	eg $15x + 20y = 50$ $15x - 18y = 69$		5	M1 for coefficients of x or y the same or for correct rearrangement of one equation followed by correct substitution in the other eg $5x - 6\left(\frac{10 - 3x}{4}\right) = 23$
		$x = 4$	$y = -\frac{1}{2}$			A1 cao dep on M1
						M1 (dep on 1st M1) for substituting for other variable
				$x = 4, y = -\frac{1}{2}$		A1 Award 4 marks for correct values if at least first M1 scored
				$(4, -\frac{1}{2})$		B1 Award 5 marks for correct answer if at least first M1 scored ft from their values of x and y
						Total 8 marks

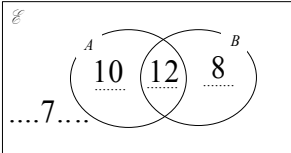
14.	(a)	55 115 155 177 190 200	1	B1	cao
	(b)		2	B1	$\pm \frac{1}{2}$ sq ft from sensible table ie clear attempt to add frequencies
		Curve or line segments		B1	ft from points if 4 or 5 correct or ft correctly from sensible table or if points are plotted consistently within each interval at the correct heights Accept curve which is not joined to the origin
	(c)	26 indicated on cf graph	2	M1	for 26 indicated on cf graph – accept 26-27 inc
		approx 60 from correct graph		A1	If M1 scored, ft from cf graph If M1 not scored, ft only from correct curve & if answer is correct ($\pm \frac{1}{2}$ sq tolerance) award M1 A1
					Total 5 marks

15.		$-4 < x < 4$	2	B2	B1 for $x < 4$ or $x > -4$ or $x < \pm 4$ or $x < \sqrt{16}$ SC B1 for $-4 \leq x \leq 4$
					Total 2 marks

16.	(a)	$\frac{3}{8} + \frac{2}{8}$ oe		2	M1	
			$\frac{5}{8}$		A1	
	(b)(i)	$\frac{2}{8} \times \frac{1}{7}$ appearing once only		5	M1	Sample space method – award 2 marks for correct answer; otherwise no marks
			$\frac{2}{56}$ or $\frac{1}{28}$		A1	for $\frac{2}{56}$ or $\frac{1}{28}$ or for 0.036 or for answer rounding to 0.036
	(ii)	$\frac{2}{8} \times \frac{3}{7} + \frac{3}{8} \times \frac{2}{7}$ or $2 \times \frac{2}{8} \times \frac{3}{7}$ oe			M1 M1	for one correct product for completely correct expression
			$\frac{12}{56}$		A1	for $\frac{12}{56}$ oe inc $\frac{3}{14}$ or for 0.21 or for answer rounding to 0.21
						Note for (b)(ii): sample space method – award 3 marks for correct answer; otherwise no marks SC M1 for $\frac{2}{8} \times \frac{3}{8}$ or $\frac{3}{8} \times \frac{2}{8}$ M1 (dep) for $\frac{2}{8} \times \frac{3}{8} + \frac{3}{8} \times \frac{2}{8}$ oe SC Sample space method – award 2 marks for $\frac{12}{64}$ oe; otherwise no marks
						Total 7 marks

17.	(a)		2	1	B1	cao
	(b)		$x < 6$	2	B2	cao B1 for eg $x \leq 6$ or ... $-2, -1, 0, 1, 2, 3, 4, 5$ SC B1 for $x \geq 6$
	(c)		7	1	B1	cao
	(d)	$g(0) = 15$		2	M1	for 15 seen
			3		A1	cao If M0, award B1 for ± 3 oe
	(e)	$k = 12$		3	M1	May be stated or indicated on diagram. May be implied by one correct solution.
			-0.7 or -0.8 3.8		A2	A1 for solution rounding to -0.7 or -0.8 A1 for solution rounding to 3.8
	(f)	$\tan$ drawn at $x = 3.5$		3	M1	$\tan$ or $\tan$ produced passes between points $(3, 3 \leq y \leq 6)$ and $(4, 11 \leq y \leq 14)$
		$\frac{\text{vertical difference}}{\text{horizontal difference}}$			M1	finds their $\frac{\text{vertical difference}}{\text{horizontal difference}}$ for two points on $\tan$ or finds their $\frac{\text{vertical difference}}{\text{horizontal difference}}$ for two points on curve, where one of the points has an x -coordinate between 3 and 3.5 inc and the other point has an x -coordinate between 3.5 and 4 inc
			6.5 – 11 inc		A1	dep on both M marks
					Total 12 marks	

18.	$(\cos x^\circ =) \frac{4^2 + 6^2 - 8^2}{2 \times 4 \times 6}$ or $8^2 = 4^2 + 6^2 - 2 \times 4 \times 6 \cos x^\circ$		3	M1 for correct substitution in Cosine Rule
	$(\cos x^\circ =) -0.25$ oe			A1
		104.5		A1 for value rounding to 104.5 (104.4775...)
				Total 3 marks

19. (a)			2	B2 for all correct B1 for 2 or 3 correct
(b)(i)		10	2	B1 cao
(ii)		25		B1 cao
				Total 4 marks

20.	$\pi \times r \times 9 = 100$ oe		5	M1
	($r =$) 3.53677...			A1 for 3.53 or for value rounding to 3.54 (3.14 $\rightarrow$ 3.53857...)
	$\sqrt{9^2 - "3.53..."^2}$			M1
	($h =$) 8.2759...			A1 for 8.27 or for value rounding to 8.28
		108		A1 for answer rounding to 108 ($\pi \rightarrow 108.40...$ 3.14 $\rightarrow$ 108.45...) If both M1s scored, award 5 marks for an answer which rounds to 108
				Total 5 marks

21.	(a)	$8y^6$	2	B2 B1 for 8 B1 for y^6
	(b)	$2^p \times (2^3)^q = 2^p \times 2^{3q} = 2^{p+3q}$	2	B2 B1 for 2^{3q} seen
				Total 4 marks

22.	(a)(i)	$3\mathbf{a} + 3\mathbf{b}$ oe	3	B1
	(ii)	$2\mathbf{a} + 2\mathbf{b}$ oe		B1 Accept eg $\frac{2}{3}(3\mathbf{a} + 3\mathbf{b})$
	(iii)	$\mathbf{a} + 2\mathbf{b}$ oe		B1 Accept eg $2\mathbf{a} + 2\mathbf{b} - \mathbf{a}$
	(b)	$\overrightarrow{DF} = 2\mathbf{a} + 4\mathbf{b}$ oe	2	M1 Also award for $\overrightarrow{EF} = \mathbf{a} + 2\mathbf{b}$ oe
		$\overrightarrow{DF} = 2 \overrightarrow{DE}$ oe eg $\overrightarrow{DE} = \overrightarrow{EF}$		A1 Also award A1 for an acceptable explanation in words.
				Total 5 marks

Further copies of this publication are available from
Edexcel Publications, Adamsway, Mansfield, Notts, NG18 4FN

Telephone 01623 467467

Fax 01623 450481

Email publication.orders@edexcel.com

Order Code UG030750 January 2012

For more information on Edexcel qualifications, please visit
www.edexcel.com/quals

Pearson Education Limited. Registered company number 872828
with its registered office at Edinburgh Gate, Harlow, Essex CM20 2JE



Llywodraeth Cynulliad Cymru
Welsh Assembly Government

